

JAWAHARLAL NEHRU TECHNOLOGICAL UNIVERSITY HYDERABAD
I B.TECH – REGULAR EXAMINATIONS, JUNE - 2010
MATHEMATICAL METHODS

(COMMON TO EEE, ECE, CSE, EIE, BME, IT, ETE, E.COMP.E, ICE)

Time: 3hours

Max.Marks:80

Answer any FIVE questions
All questions carry equal marks

- - -

- 1.a) Find the Rank of the Matrix, by reducing it to the normal form

$$\begin{bmatrix} 2 & 1 & 3 & 5 \\ 4 & 2 & 1 & 3 \\ 8 & 4 & 7 & 13 \\ 8 & 4 & -3 & -1 \end{bmatrix}$$

- b) Find whether the following system of equations are consistent. If so solve them.
 $x + y + 2z = 9$, $x - 2y + 2z = 3$, $2x - y + z = 3$, $3x - y + z = 4$. [8+7]

2. Verify Cayley Hamilton theorem and find the inverse of

$$\begin{bmatrix} 1 & 3 & 7 \\ 1 & 2 & 3 \\ 1 & 2 & 1 \end{bmatrix}$$

[15]

3. Reduce the quadratic form to the canonical form
- $x^2 + y^2 + 2z^2 - 2xy + 4zx + 4yz$
- [15]

- 4.a) Find a real root of the equation
- $e^x \sin x = 1$
- using Newton Raphson method.

- b) Find $y(10)$, Given that $y(5) = 12$, $y(6) = 13$, $y(9) = 14$, $y(11) = 16$ using Lagrange's formula. [8+7]

- 5.a) Using the method of least squares find the constants
- a
- and
- b
- such that
- $y = ae^{bx}$
- fits the following data:

x	0	0.5	1	1.5	2	2.5
y	0.10	0.45	2.15	9.15	40.35	180.75

- b) Obtain a relation of the form $y = ab^x$ for the following data by the method of least squares. [7+8]

x	2	3	4	5	6
y	8.3	15.4	33.1	65.2	127.4

6. Solve
- $\frac{dy}{dx} = xy + 1$
- and
- $y(0) = 1$
- using Taylor's series method and compute
- $y(0.1)$
- . [15]

- 7.a) If
- $f(x) = \cosh ax$
- expand
- $f(x)$
- as a Fourier Series in
- $(-\Pi, \Pi)$
- .

- b) Expand the Function $f(x) = x^3$ as a Fourier Series in $-\Pi < x \leq \Pi$. [7+8]

- 8.a) Solve
- $(z^2 - 2yz - y^2)p + (xy + zx)q = xy - zx$
- .

- b) Find the integral surface of $x(y^2 + z)p - y(x^2 + z)q = (x^2 + y^2)z$. [7+8]